



U.S. Army Conference on Applied Statistics, 20-22 October, 2004



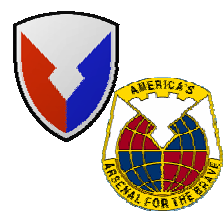
Evaluation of Advanced Aerospace Aluminum Alloys For Armor and Structural Applications

Reference: ARL-TR-3185

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Introduction



Solutions to High Fuel and Material Costs

Materials, Processing, and Performance Improvements

- **Durability**
- **Specific-Strength and Toughness**
- **Low Material and Operating Costs**
- **Isotropic Mechanical Properties**
- **Weldable Al-Cu-Li Alloys**

Lithium as Alloy-Element

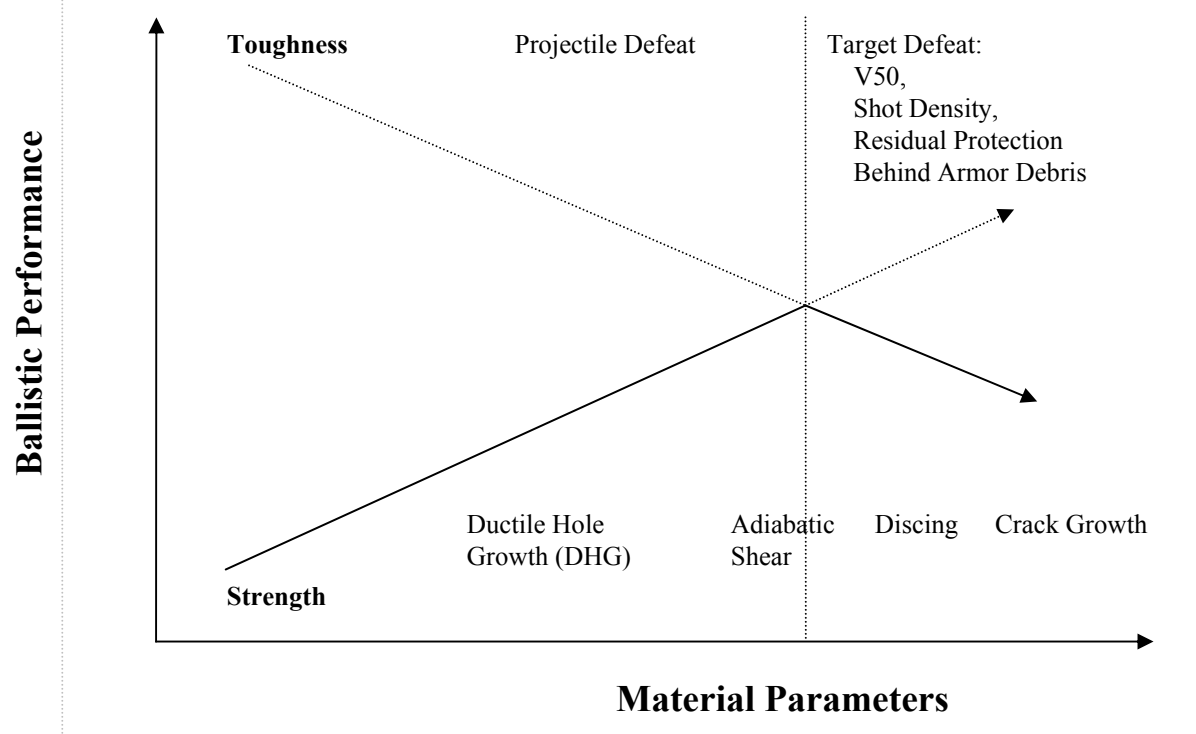
- **Non-Toxic**
- **3% Density-Reduction / Weight-%**
- **6% Elastic Modulus Increase / Weight-%**



Introduction



Aluminum Armor: Material Parameters and Ballistic Performance of Small-Caliber Projectiles



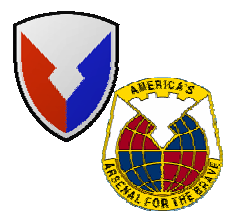
- Plastic Flow, and Failure Modes Determine Performance
- At High-Strength Levels, Localization of Plastic Flow and Fracture Decrease Ballistic Performance



Introduction

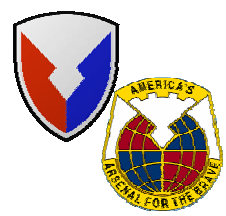


- **Al-Li Alloys versus Al-Armor 7039**
 - **Literature: Investigations Controversial-**
 - a. **2090-T8: No significant improvement, either at 0° or 30°;**
 - b. **2090-T8: Improvement claimed with 0° impact obliquity, but not oblique; Al-Li material parameters claimed significant**
 - c. **2090-T8 & 2049 Improvement claimed at 30° obliquity, effect improves with strength.**
- **Quantitatively,**
 - What are the V50 mean and variance of 7039 Al-armor performance?**
 - Do the experimental materials provide significant V50 improvements?**
 - What are the improvements?**
- **Do the material parameters or failure modes enhance ballistic protection?**



Experimental Aluminum Alloy Target Materials

- C47A, C458 Al-Cu-Li-Zn (C458 → 2099)
- 7055 Al-Zn-Cu-Mg
- 2195 Al-Cu-Li-Mg-Ag



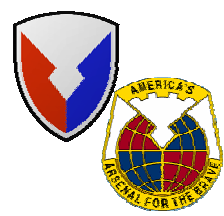
Experimental Results

Experimental Mechanical Properties In Tension with Range Variation - Comparison to Reference Alloys

Property	Experimental Alloys and Tempers				Reference Data:Al Armor and Al-Li		
	C47A -T8	C458 -T861	2195 -T8	7055 -T7751	7039 -T64	2519 -T87	2090 -T8
Young's Modulus (GPa)	76.8 (0.6)	77.7 (0.4)	75.9 (0.6)	70.6 (0.6)	70	72	79
0.2% Yield Strength (MPa)	437 (4.2)	525 (5.2)	592 (1.8)	602 (1.9)	400	423	490
Ultimate Strength (MPa)	469 (1.5)	558 (2.7)	627 (0.9)	632 (2.1)	458	465	550
Elongation (%)	13.2 (1.7)	9.3 (1.4)	9.6 (2.7)	14.5 (0.7)			
Reduction of Area (%)	44.3 (0)	23.5 (7.1)	22.2 (9.1)	40.7 (1.1)			

Experimental Results: average of 3 specimens strained to failure,
except C458 = 6 specimens

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Experimental Results

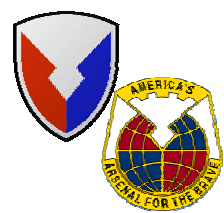


Physical Properties And Specific Strength

Property	Experimental Alloy				Al Armor			Ti Armor
	C47A-T8	C458-T861	2195-T8	7055-T7751	5083	7039	2519	6Al-4V
Density (ρ), (g/cm ³)	2.642	2.633	2.709	2.866	2.66	2.73	2.82	4.43
Hardness (HRB)	75.0	80.4	88.3	92.1	—	—	—	—
Young's Modulus (GPa)	76.8	77.7	75.9	70.6	70.3	69.6	72.4	110
Specific Modulus (E/ρ)/10 ⁻⁸ (cm)	2.96	3.01	2.86	2.51	2.69	2.60	2.62	2.53
Specific Strength (YS/ρ)/10 ⁻⁶ (cm)	1.69	2.03	2.23	2.14	1.20	1.45	1.53	1.75–2.10

- Al-Cu-Li Alloys Have the Highest Specific Modulus and Strength

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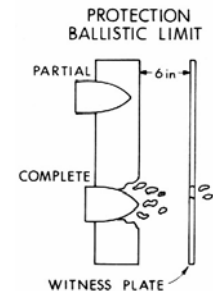


Experimental Results



Ballistic V50 Test: Procedure, Results, Criteria

Test Criteria



Projectile		Target Characteristics			Penetration Result Intervals		V50 Prot. Limit	
Type	Impact Obliquity (°)	Alloy	Thickness (t) (mm)	AD (kg/m ²)	Target Impacts (No.)	Distribution of All P, C, Penetrations	Averaged	
							Shots (No.)	(S) Spread (m/s)
0.50-cal. FSP	0	C47A	19.10	50.46	8 UM	$3P \leq S \leq 5C$	2	1.2
	0	2195	19.13	51.83	5 UM	$3P \leq S \leq 2C$	2	2.4
	0	C458	19.91	52.43	8 M	$3P \leq S \leq 3C$	4	15.8
20-mm FSP	0	7055	31.72	90.95	5 UM	$3P \leq S \leq 2C$	2	5.8
	0	2195	40.16	108.8	6 UM	$4P \leq S \leq 2C$	2	17.7
0.30-cal. APM2	0	C47A	19.02	50.26	10 UM	$7P \leq S \leq 3C$	2	2.7
	0	2195	19.11	51.76	4 M	$1P \leq S \leq 1C$	4	15.5
	0	C458	19.91	52.43	6 UM	$3P \leq S \leq 3C$	2	11.0
	0	7055	18.95	54.34	4 UM	$2P \leq S \leq 2C$	2	4.9
	0	2195	31.76	86.02	9 UM	$4P \leq S \leq 5C$	2	4.3
	0	7055	31.75	91.03	11 UM	$8P \leq S \leq 3C$	2	3.7
	0	2195	40.18	108.9	11 UM	$7P \leq S \leq 4C$	2	13.4
	30	C47A	19.08	50.40	10 M	$3P \leq S \leq 3C$	6	23.2
	30	2195	19.11	51.76	12 M	$4P \leq S \leq 3C$	4	20.4
	30	C458	19.94	52.50	9 M	$4P \leq S \leq 3C$	4	17.4
	45	C458	19.90	52.40	12 UM	$9P \leq S \leq 3C$	2	7.9
0.50-cal. APM2	0	2195	39.65	107.4	9 UM	$5P \leq S \leq 4C$	4	7.9

UM = UnMixed, all P or all C results

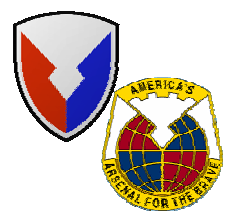
M = Mixed, includes P & C results

P = Partial Penetration

C = Complete Penetration

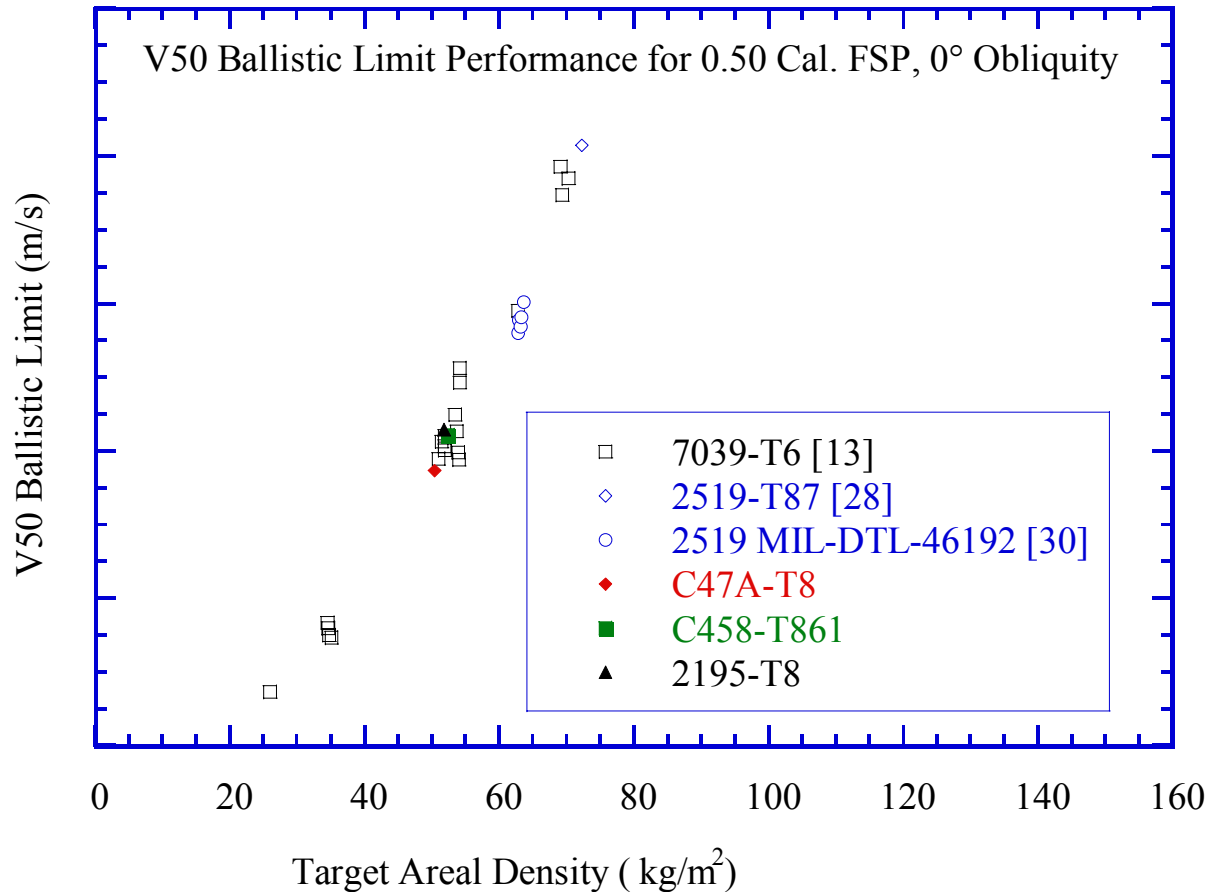
S = spread, range of velocities of P and C results used in V50 estimate

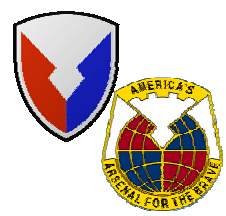
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Results - Discussion

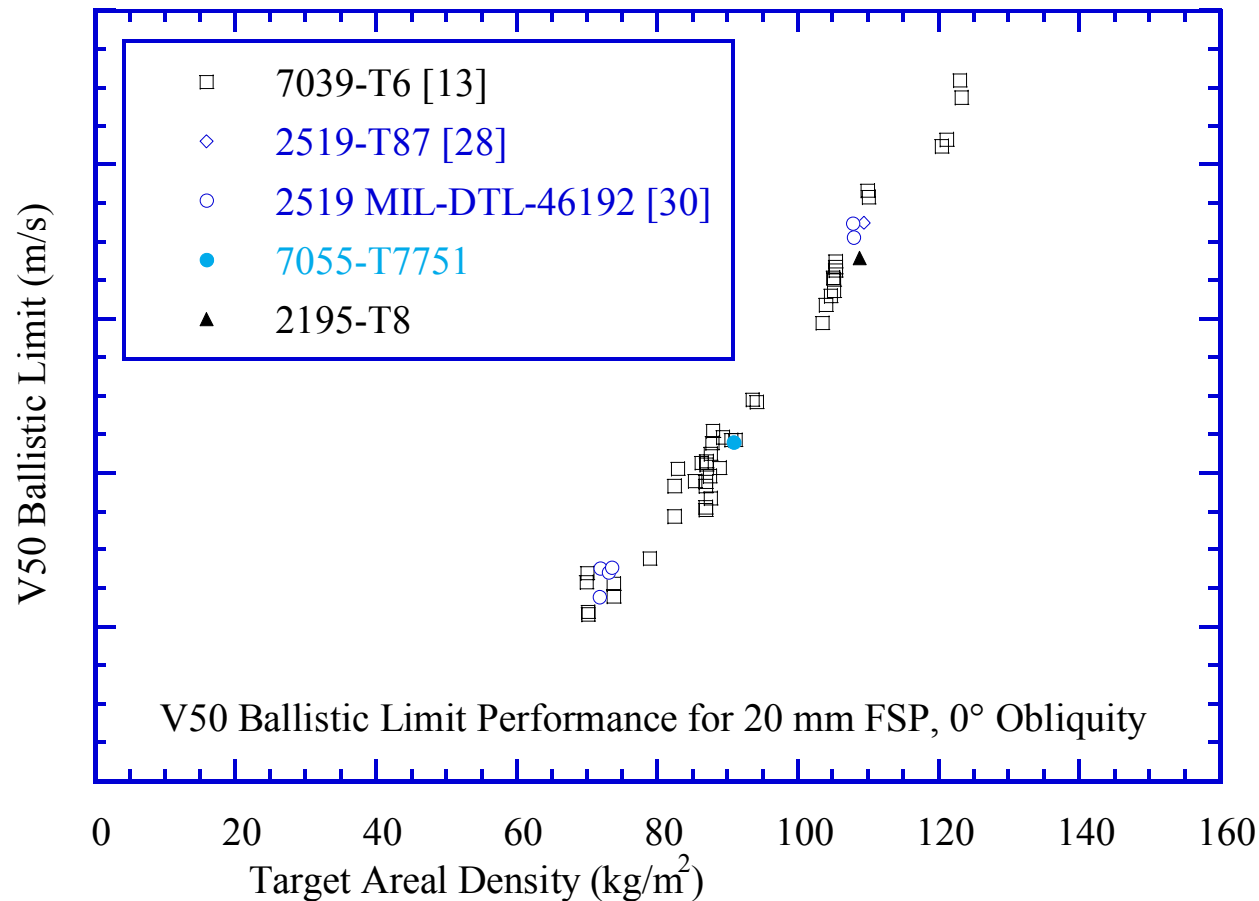
0.50 cal. FSP, 0° Obliquity





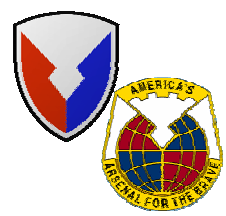
Results - Discussion

20 mm FSP, 0° Obliquity



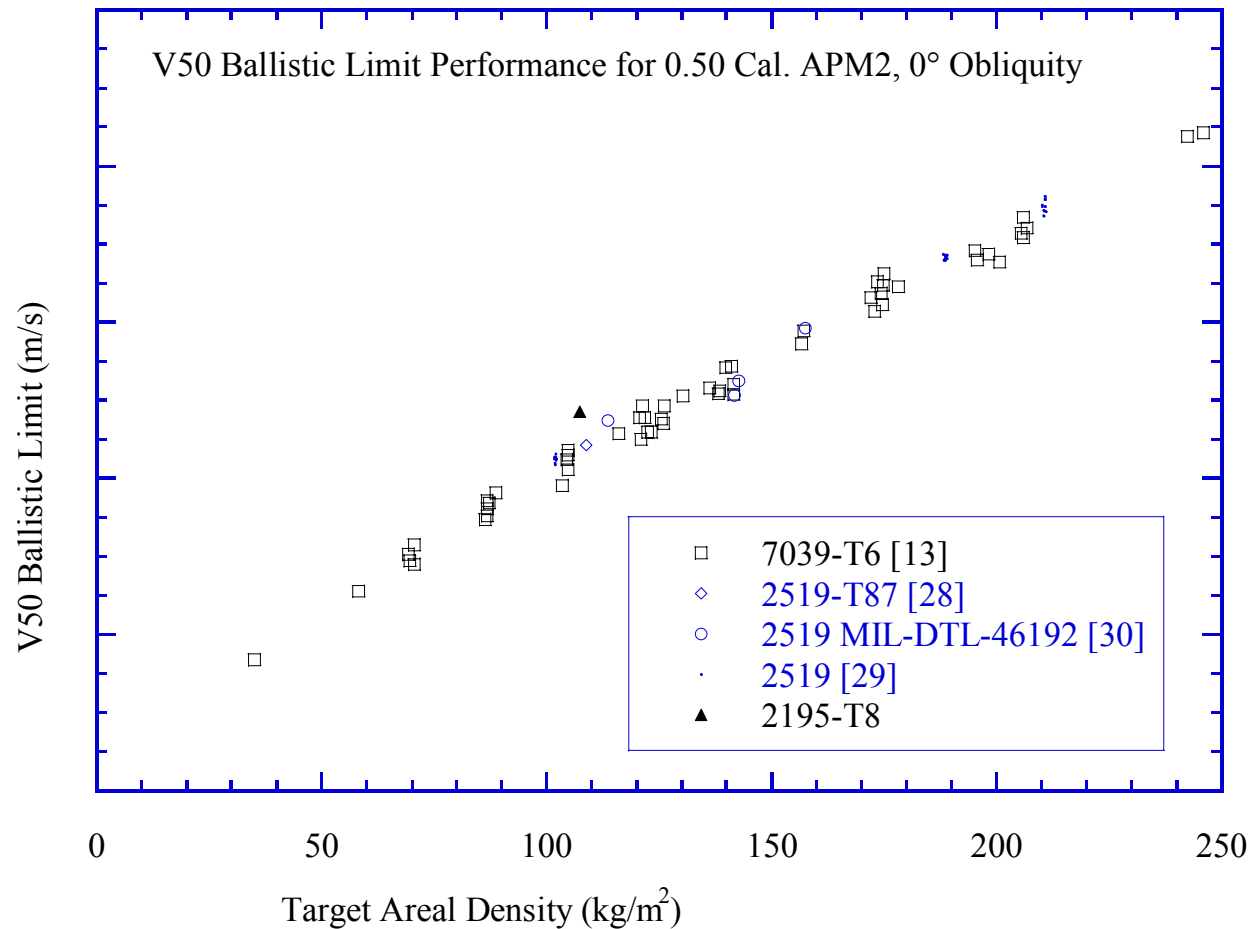
Experimental Alloys with 7039 and 2519 Al armor V50 Performance

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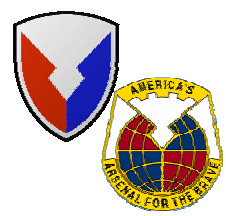
Results - Discussion

0.50 cal. APM2, 0° Obliquity



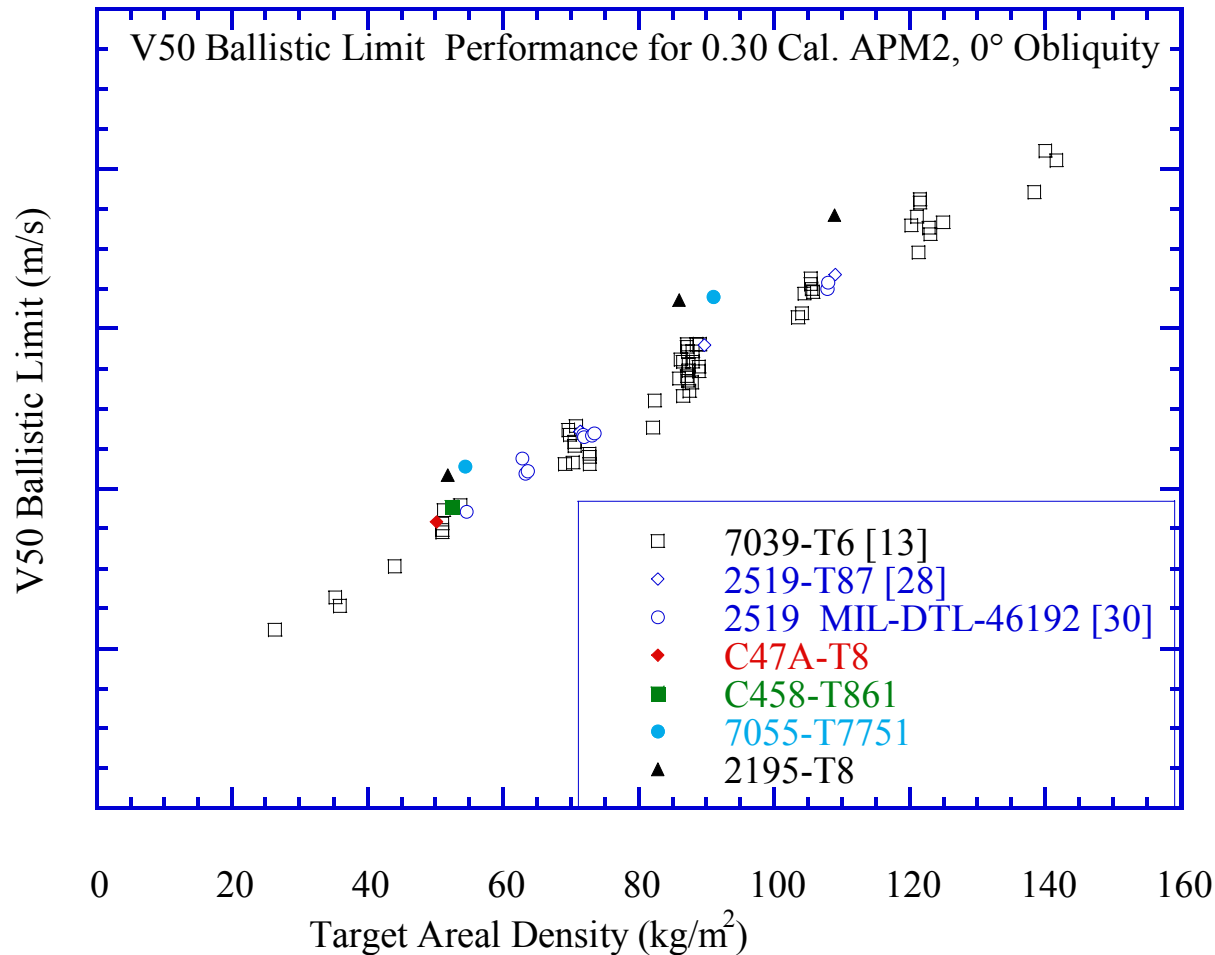
Experimental Alloys with 7039 and 2519 Al armor V50 Performance

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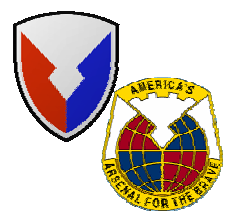
Results - Discussion

0.30 cal. APM2, 0° Obliquity



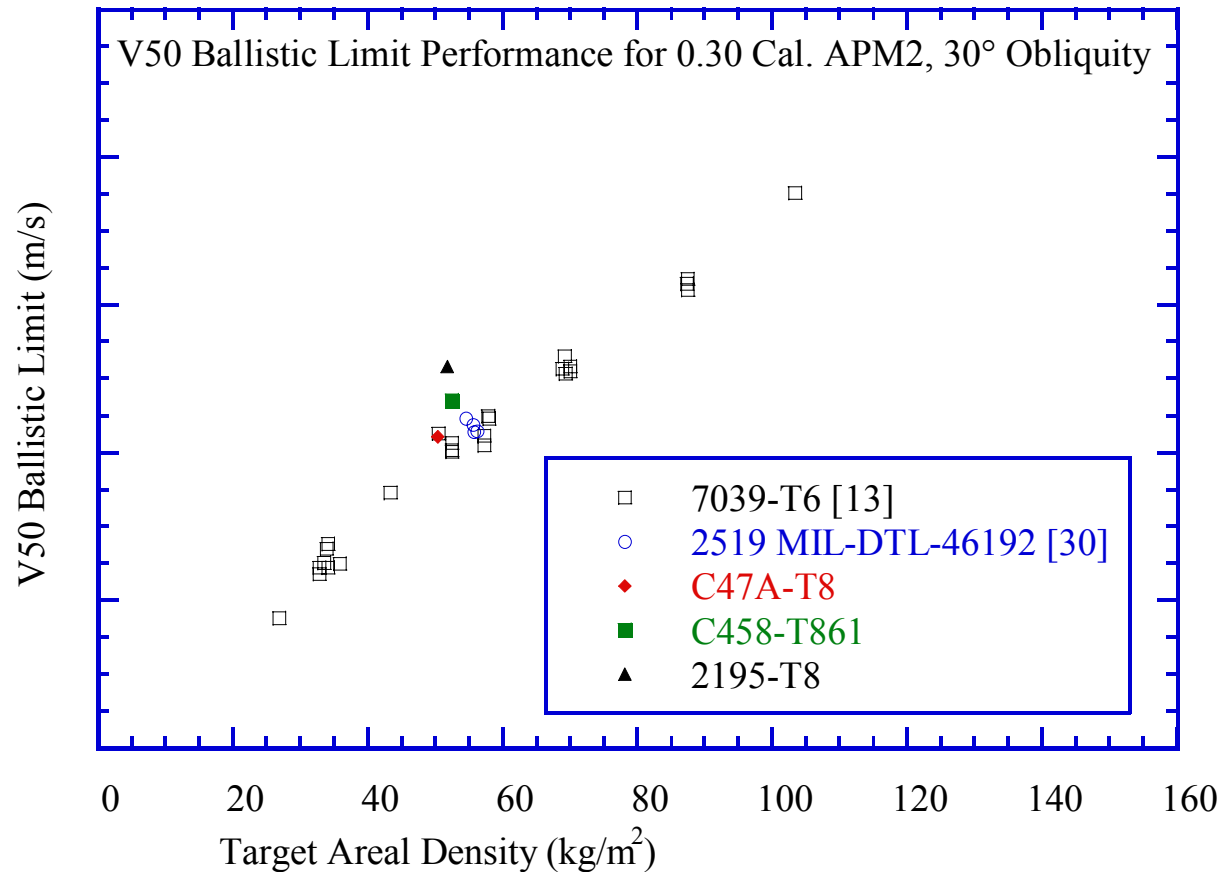
Experimental Alloys with 7039 and 2519 Al armor V50 Performance

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Results - Discussion

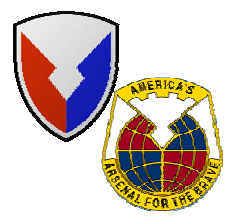
0.30 cal. APM2, 30° Obliquity



Experimental Alloys with 7039 and 2519 Al armor V50 Performance

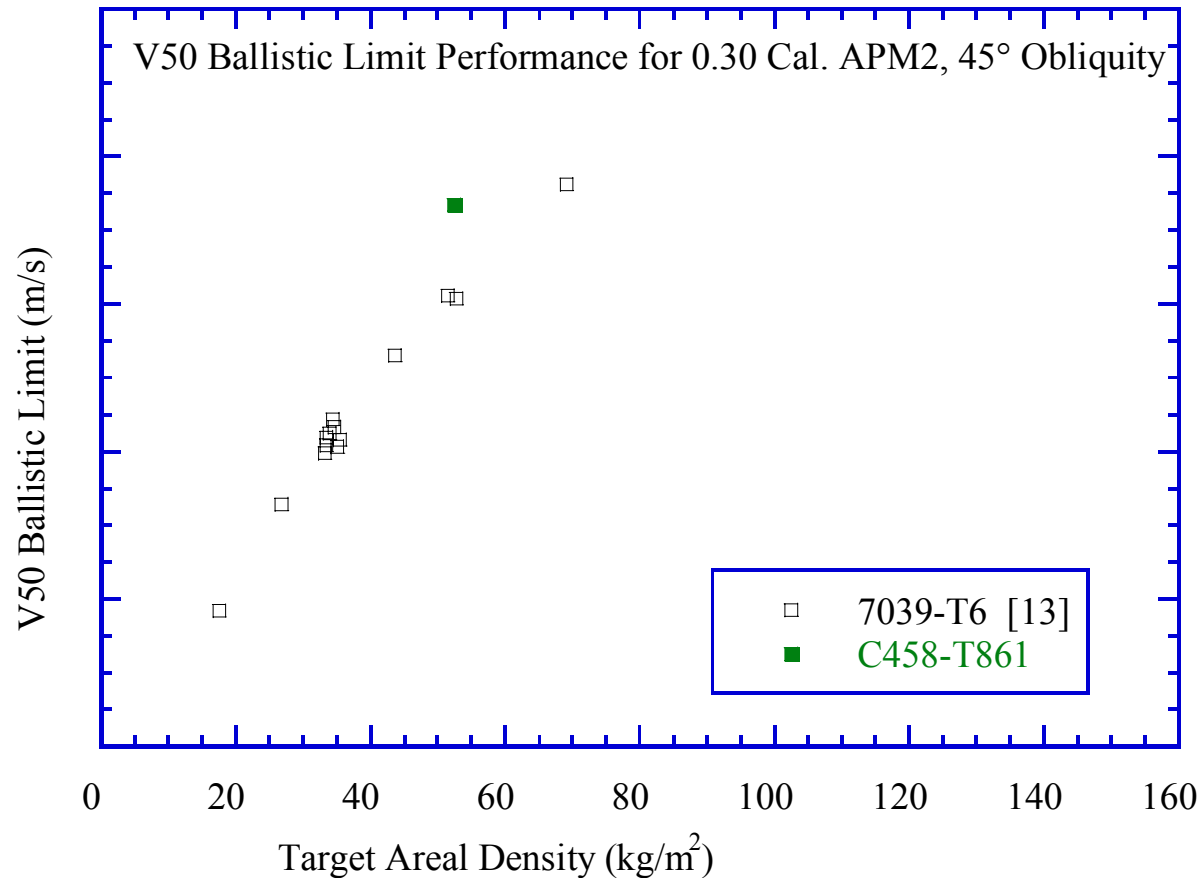
- Oblique-Impact V50 Performance of Al-Li Alloys > 7039

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Results - Discussion

0.30 cal. APM2, 45° Obliquity

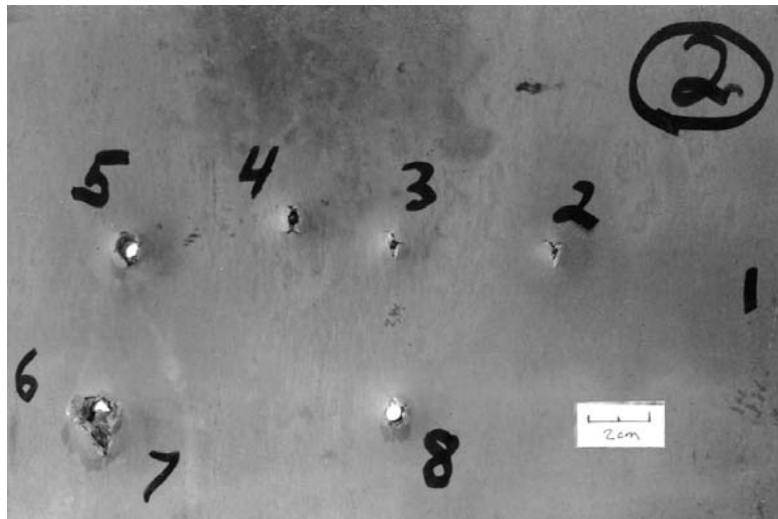


Experimental Alloys with 7039 and 2519 Al armor V50 Performance

- Oblique-Impact V50 Performance of Al-Li Alloys > 7039

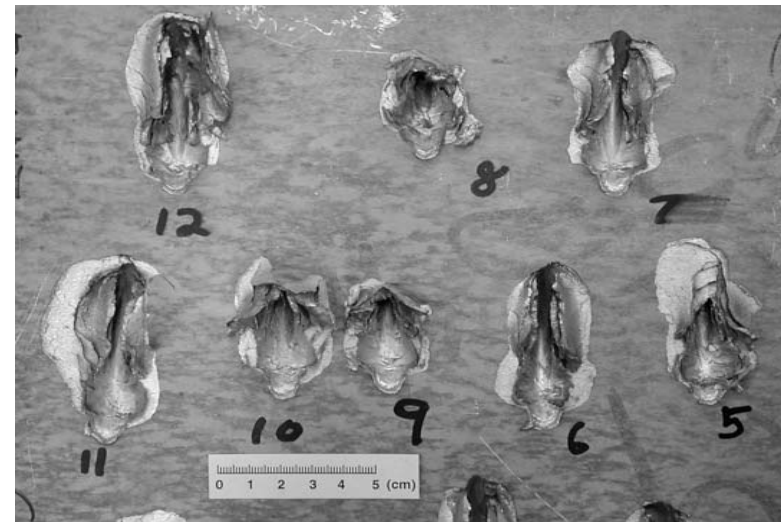
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0.30 cal. APM2 Penetration Modes



C458-T861: 0° Obliquity

- Damage-tolerant
- High shot-density
- Multiple impacts



C458-T861: 45° Obliquity

$$V50\ 45^\circ = 1.62 \times V50\ 0^\circ$$



Results and Discussion

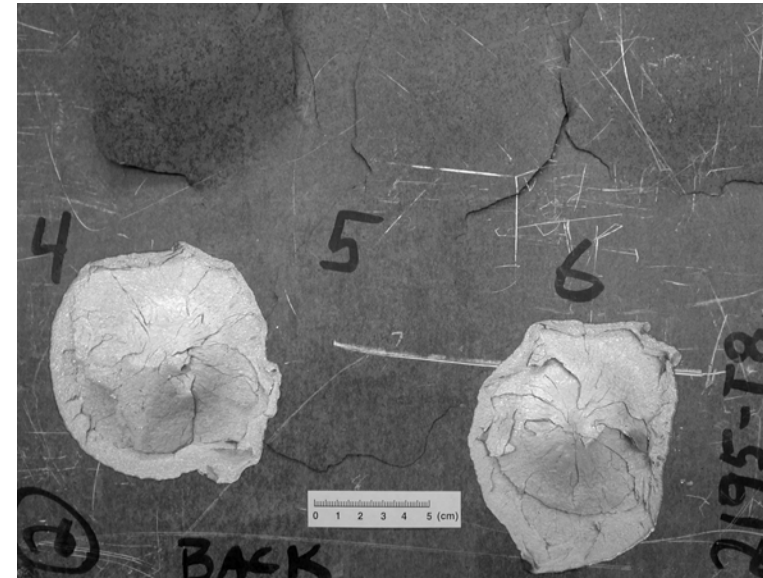


FSP Penetration Mode



C47A-T8 versus 0.50 cal. FSP

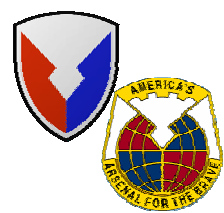
- Damage-tolerant
- High shot-density
- Multiple impacts



2195-T8 versus 20 mm FSP

- Ductile Hole Growth
+ Discing Failure

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Results and Discussion



Linear Regression in Matrix Notation

$\mathbf{Y} = \mathbf{X} \boldsymbol{\beta} + \boldsymbol{\varepsilon}$ Model with k order or regression variables, $p = k + 1$ regression coefficients (parameters)

$\beta_j, j = 0, 1, 2, \dots, k$, $\mathbf{Y} = n \times 1$ vector of observed values, $\mathbf{X} = n \times p$ matrix of levels of regressor variable(s), $\boldsymbol{\beta} = p \times 1$ vector of regression coefficients, $\boldsymbol{\varepsilon} = n \times 1$ vector of random errors

$$(\mathbf{X}'\mathbf{X})\hat{\boldsymbol{\beta}} = \mathbf{X}'\mathbf{Y}$$

Normal equations

$$\hat{\boldsymbol{\beta}} = (\mathbf{X}'\mathbf{X})^{-1} \mathbf{X}'\mathbf{Y}$$

Parameter estimates

$$\hat{\mathbf{Y}} = \mathbf{X}\hat{\boldsymbol{\beta}}$$

Fitted values (mean-estimates) corresponding to observed values, $\mathbf{Y}$

$$= \mathbf{X}(\mathbf{X}'\mathbf{X})^{-1} \mathbf{X}'\mathbf{Y}$$

“Hat matrix” maps vector of observed values into vector of fitted values

$$= \mathbf{H}\mathbf{Y}$$

$$\mathbf{e} = \mathbf{Y} - \hat{\mathbf{Y}} = (\mathbf{I} - \mathbf{H})\mathbf{Y}$$

Residuals, vector of residual errors $\mathbf{e}$

$$\text{Var}(\hat{\boldsymbol{\beta}}) = (\mathbf{X}'\mathbf{X})^{-1} \sigma^2$$

Variance of $\hat{\boldsymbol{\beta}}$

$$\text{Var}(\hat{\mathbf{Y}}) = \mathbf{X}[\text{Var} \hat{\boldsymbol{\beta}}] \mathbf{X}'$$

Variance of all mean estimates, $\hat{\mathbf{Y}}$

$$= \mathbf{X}(\mathbf{X}'\mathbf{X})^{-1} \mathbf{X}' \sigma^2 = \mathbf{H} \sigma^2$$

$$\text{Var}(\hat{\mathbf{Y}}_{\text{pred}}) = (\mathbf{I} + \mathbf{H}) \sigma^2$$

Variance of prediction, single point future

$$\text{Var}(\mathbf{e}) = (\mathbf{I} - \mathbf{H}) \sigma^2$$

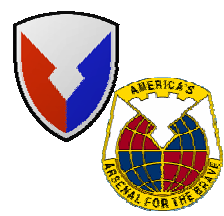
Variance of the residual errors

$$\mathbf{Y}'\mathbf{Y} - n\bar{Y}^2 = (\hat{\boldsymbol{\beta}}'\mathbf{X}'\mathbf{Y} - n\bar{Y}^2) + (\mathbf{Y}'\mathbf{Y} - \hat{\boldsymbol{\beta}}'\mathbf{X}'\mathbf{Y})$$

Total sum of squares (corrected)

partitioned into errors due to

regression + residual, $S_{yy} = SS_R + SS_E$



Results and Discussion



Regression in Matrix Notation

$$R_a^2 = 1 - \frac{SS_E/n - p}{S_{yy}/n - 1}$$

Coefficient of determination

$$= 1 - \frac{n - 1}{n - p} (1 - R^2)$$

Adjusted coefficient of determination

$$\frac{S_{yy}}{n - 1} = \frac{SS_R}{k} + \frac{SS_E}{n - p}$$

Mean sums of squares partitioned, corrected,
 $k = p - 1$, k = variables n = observations, p = coefficients

$$MS_E = \frac{SS_E}{n - (k + 1)} = \frac{SS_E}{n - p}$$

the residual mean square s^2 , a model-dependent estimate of variance σ^2 , where

$$SSE = \sum_{i=1}^n e_i^2 = \mathbf{Y}'\mathbf{Y} - \hat{\boldsymbol{\beta}}'\mathbf{X}'\mathbf{Y}$$

$$T = \frac{\hat{Y}_0 - \mu_{Y|1, x_{01}, x_{02}, \dots, x_{0k}}}{s \sqrt{\mathbf{x}'_0 (\mathbf{X}'\mathbf{X})^{-1} \mathbf{x}_0}}$$

statistic for construction of 100(1- α)% confidence intervals on the mean (predicted) response $\mu_Y = | 1, x_{01}, x_{02}, \dots, x_{0k}$ where s^2 is an estimate of the variance σ^2 , $\mathbf{x}_0$ or $\mathbf{x}'_0 =$

$[1, x_{01}, x_{02}, \dots, x_{0k}]$ is the condition vector, and where the statistic is T distribution probability determined by degrees of freedom $\nu = n - p = n - k - 1$

$$s(\hat{Y}_0) = \sqrt{\mathbf{x}'_0 (\mathbf{X}'\mathbf{X})^{-1} \mathbf{x}_0 s^2}$$

Conditional standard error on the mean estimate (response)

$$s(\hat{Y}_0 - Y_0) = \sqrt{(\mathbf{1} + \mathbf{x}'_0 (\mathbf{X}'\mathbf{X})^{-1} \mathbf{x}_0) s^2}$$

Conditional standard error for a single point future prediction on an observed response

¹ Walpole, R. E.; Myers, R. H.; Myers, 1972.

² Montgomery, D. C.; Peck, 1992.

³ Rawlings, J. O. 1988.

⁴ Gerald, C. F. 1980.



Discussion



Summarize & Predict V50 Performance of 7039-T6 Armor,

Mean Estimates and Confidence Intervals,

Independent Variable = Areal Density(AD) the Target Weight / Unit Area

$$V50_{i7039-T6} = \beta_0 + \beta_1 AD_i + \beta_2 AD_i^2 + [\beta_3 AD_i^3] \quad (\text{Mathematica v2.2})$$

Polynomial Least Square (LS) Regression, Coefficients and Statistics

Projectile		Polynomial Regression, 7039-T6 V50 Ballistic Performance f(AD)								
Type	Obl. (°)	Obs. (n)	R ² _a	s (m/s)	Coefficient Estimates				t Dist. t (1-0.025, v)	d.f. (v)
					B ₀	B ₁	B ₂	B ₃		
0.50-cal. FSP	0	23	0.99170	32.36	XXX.xxx	-XX.xxxx	0.xxxxxx	-0.00xxxxxx	2.093	19
20-mm FSP	0	44	0.98110	25.76	XXX.xx	-XX.xxx	0.xxxxxx	-0.00xxxxxx	2.021	40
0.30-cal. APM2	0	58	0.98090	19.69	XXX.xxx	X.xxxx	0.0xxxxx	-0.000xxxxx	2.005	54
	30	26	0.99100	14.09	-XX.xxxx	XX.xxxx	-0.xxxxxx	0.00xxxxxx	2.074	22
	45	14	0.99087	13.22	XXX.xxx	XX.xxxx	-0.0xxxxx	—	2.201	11
0.50-cal. APM2	0	55	0.99180	13.53	XXX.xxx	X.xxxxx	-0.00xx	0.0000xxxx	2.008	51

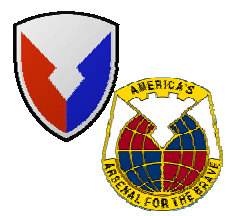
Notes: s = standard error

t = critical values of t-distribution for determination of a two-tailed 95% confidence interval

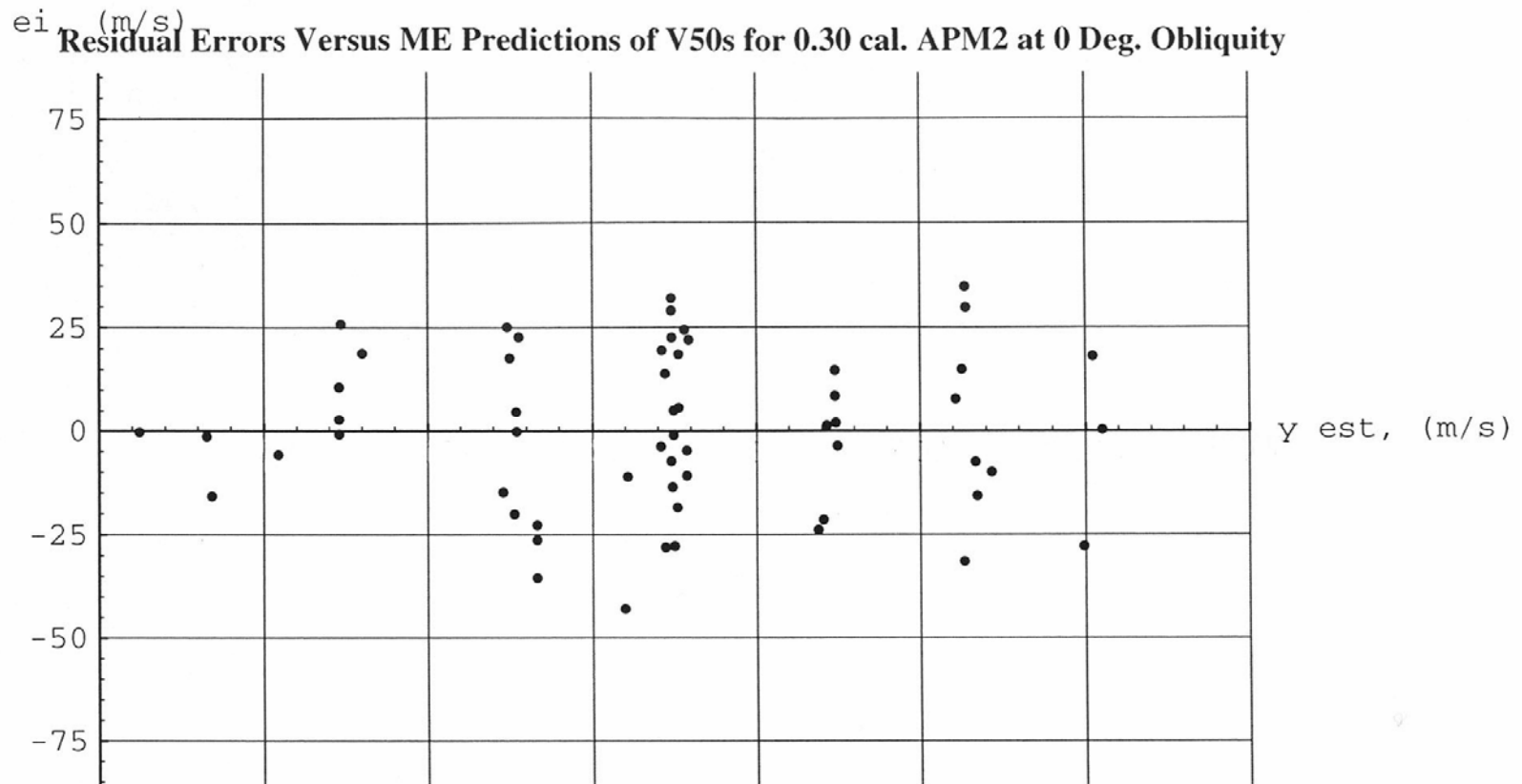
v = degrees of freedom

R²_a = adjusted coefficient of determination

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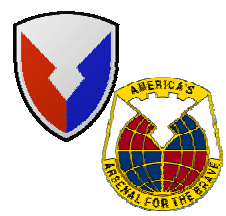


Discussion



Plot of residuals versus fitted regression values of 7039-T6 V50s

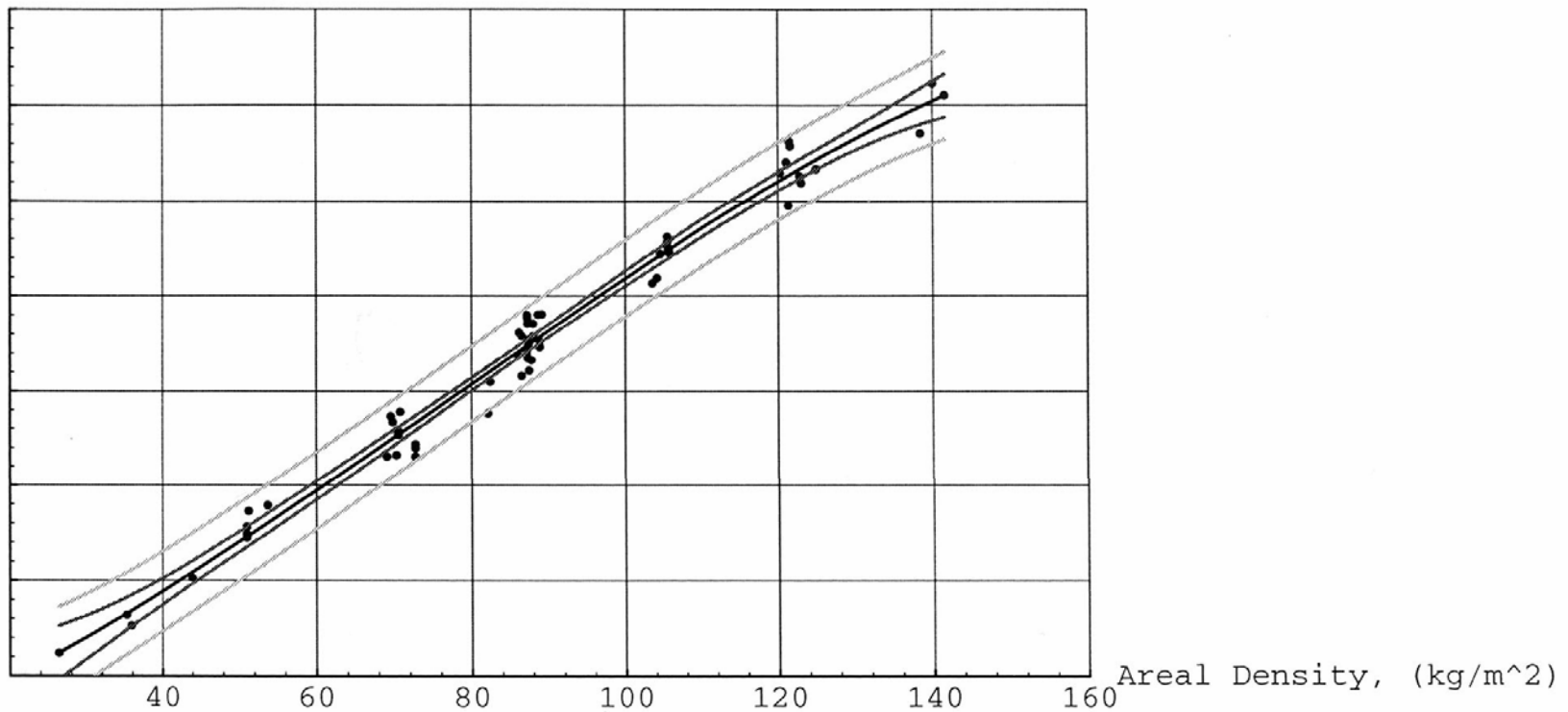
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Discussion



V-50, (m/s) 7039 Observations, V50 MEs, and 95% CLs for MEs and SPPFs



7039-T6 V50 observations, $n = 58$, and 95% CLs for mean estimates (MEs), and single point future predictions (SPPFs)

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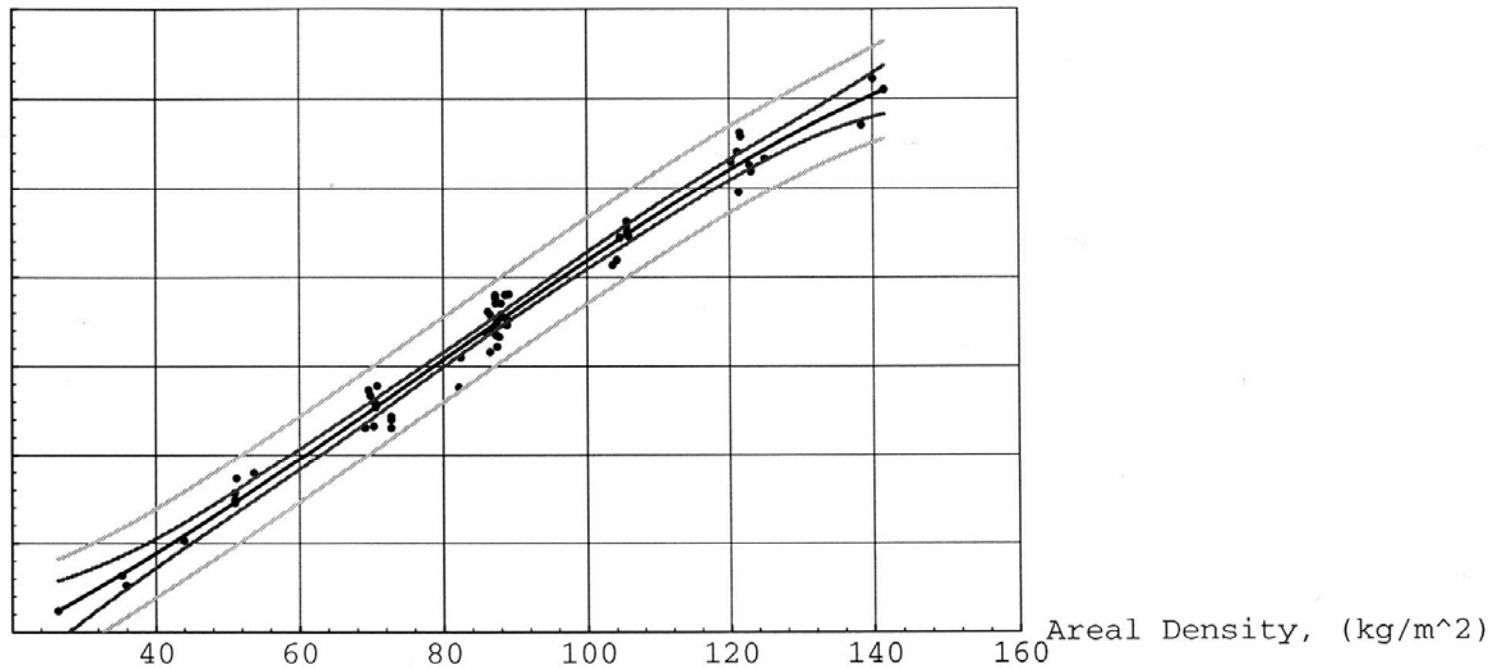


Discussion



V-50, (m/s)

7039 Observations, V50 MEs, and 98% CLs for MEs and SPFPs



7039-T6 V50 observations, $n = 58$, and 98% CLs for mean estimates (MEs), and single point future predictions (SPFPs)

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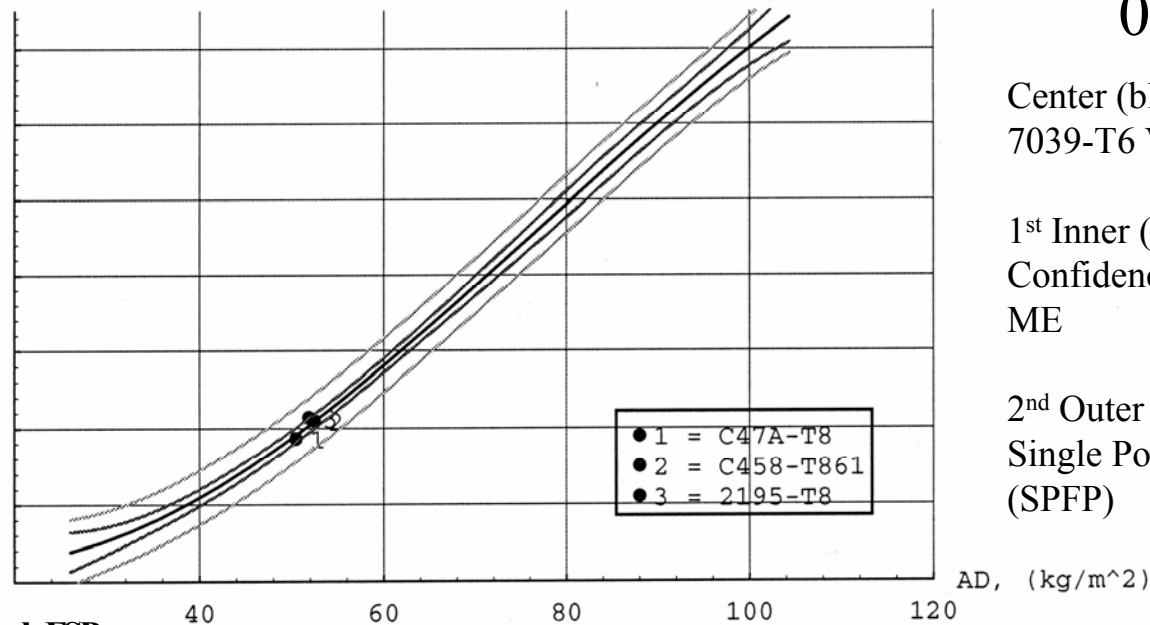


Discussion



Comparisons to 7039-T6 V50 Performance: LS Regression

V50, m/s
0.50 Cal. FSP, 0° Obliquity: Experimental Results Versus 7039-T6 Mean Estimates and 95% CLs



0.50 cal. FSP, 0°

Center (black) line = Predicted Mean
7039-T6 V50 Estimate, (ME)

1st Inner (gray) lines = 7039-T6 ME
Confidence Interval Limits = 95% (CL)
ME

2nd Outer (gray) lines = 7039-T6 CL
Single Point Future Prediction = 95% CL
(SPFP)

0.50 cal. FSP

Exp. Results Vs 7039-T6 Mean V50 Estimates and Confidence Interval Limits of the Mean and Single Point Future Prediction

Alloy	AD	V50-VME7039	Conditional	Conditional	t	ME 95%CL	SPFP 95%CL
(i)	(kg/m ²)	(m/s)	s, mean	s, pred		(± m/s)	(± m/s)
			m/s)	(m/s)			
1	50.46	-8.489	9.238	33.65	-0.2523	19.33	70.44
3	51.83	21.83	9.032	33.6	0.6499	18.9	70.32
2	52.43	3.622	8.947	33.57	0.1079	18.73	70.27

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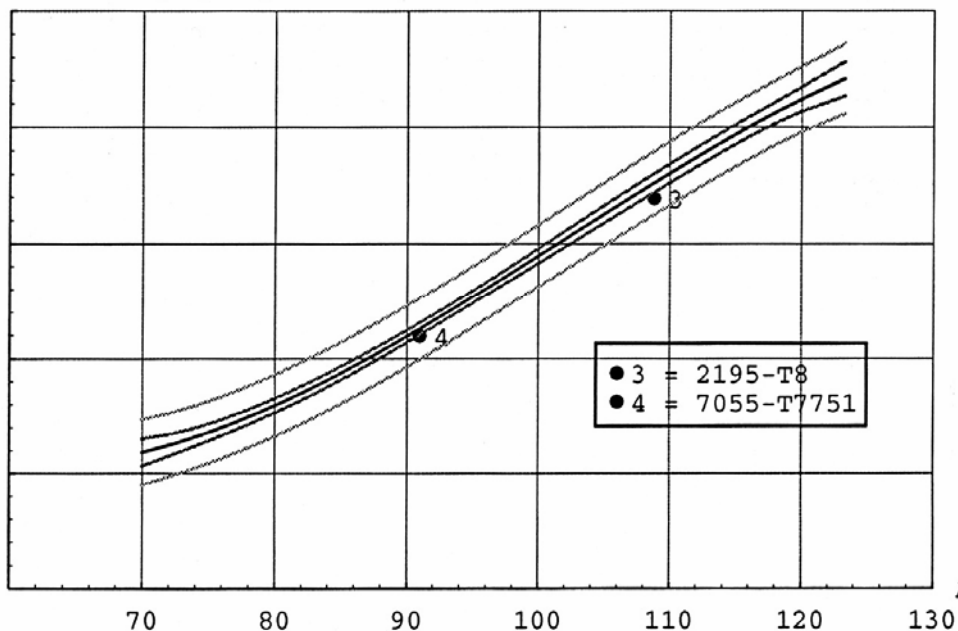


Discussion



Comparisons to 7039-T6 V50 Performance: LS Regression

V50, m/s
20 mm FSP, 0° Obliquity: Experimental Results Versus 7039-T6 Mean Estimates and 95% CLs



20 mm FSP, 0°

Center (black) line = Predicted Mean
7039-T6 V50 Estimate, (ME)

1st Inner (gray) lines = 7039-T6 ME
Confidence Interval Limits = 95% (CL)
ME

2nd Outer (gray) lines = 7039-T6 CL
Single Point Future Prediction = 95% CL
(SPFP)

20 mm FSP

Exp. Results Vs 7039-T6 Mean V50 Estimates and Confidence Interval Limits of the Mean and Single Point Future Prediction

Alloy	AD	V50-VME7039	Conditional	Conditional		ME 95% CL	SPFP 95% CL
(i)	(kg/m ²)	(m/s)	s, mean	s, pred	t	(± m/s)	(± m/s)
			(m/s)	(m/s)			
4.	90.95	-12.39	5.186	26.28	-0.4715	10.48	53.11
3.	108.8	-26.13	7.944	26.96	-0.9691	16.06	54.49

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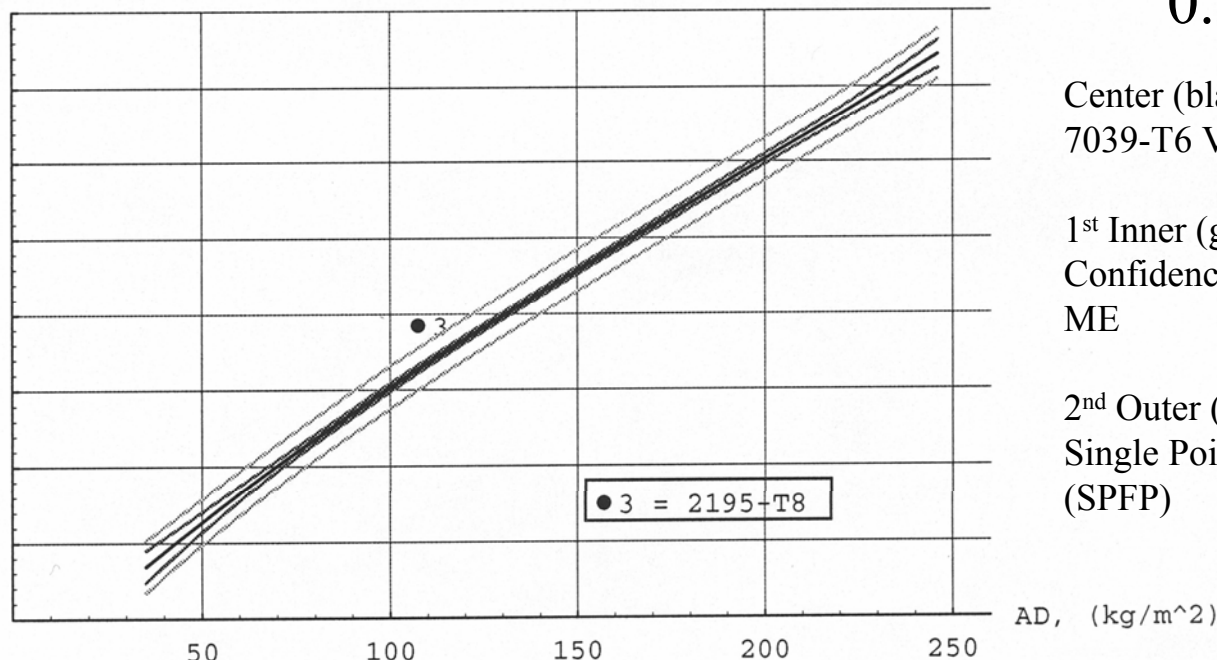


Discussion



Comparisons to 7039-T6 V50 Performance: LS Regression

V50, m/s
0.50 Cal. APM2, 0° Obliquity: Experimental Results Versus 7039-T6 Mean Estimates and 95% CLs



0.50 cal. APM2, 0°

Center (black) line = Predicted Mean
7039-T6 V50 Estimate, (ME)

1st Inner (gray) lines = 7039-T6 ME
Confidence Interval Limits = 95% (CL)
ME

2nd Outer (gray) lines = 7039-T6 CL
Single Point Future Prediction = 95% CL
(SPFP)

50 cal. APM2

Exp. Results Vs 7039-T6 Mean V50 Estimates and Confidence Interval Limits of the Mean and Single Point Future Prediction

Alloy	AD	V50-VME7039	Conditional s, mean	Conditional s, pred	t	ME 95% CL	SPFP 95% CL
(i)	(kg/m ²)	(m/s)	(m/s)	(m/s)		(± m/s)	± m/s)
3.	107.4	57.76	2.7	13.8	4.186	5.42	27.7

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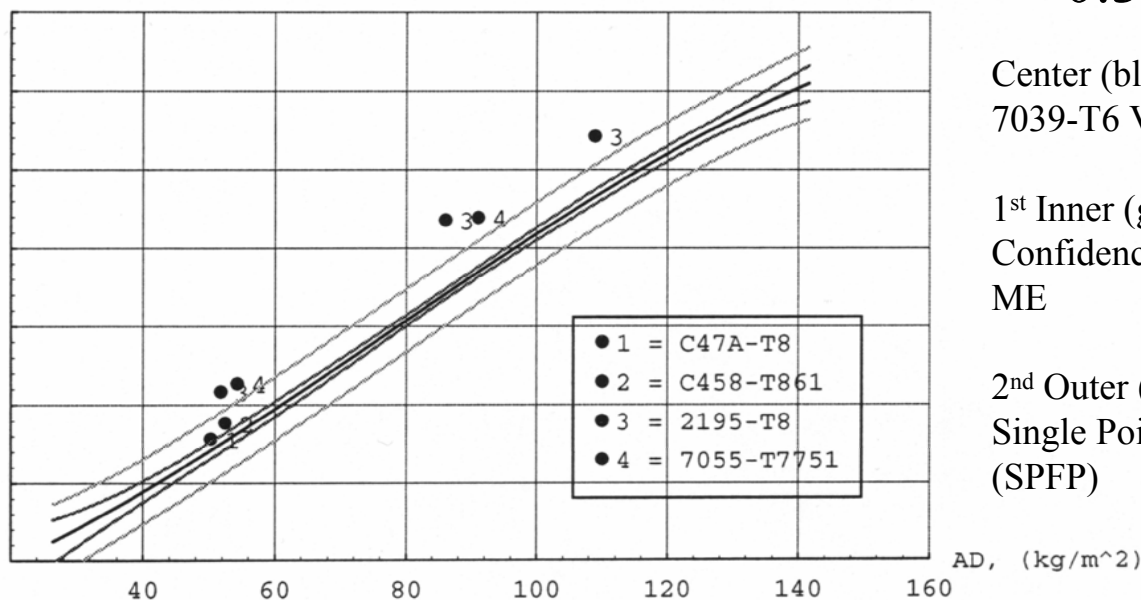


Discussion



Comparisons to 7039-T6 V50 Performance: LS Regression

V50, m/s
0.30 Cal APM2, 0° Obliquity: Experimental Results Versus 7039-T6 Mean Estimates and 95% CLs 0.30 cal. APM2, 0°



0.30 cal. APM2, 0° Obliquity

Exp. Results Vs 7039-T6 Mean V50 Estimates and Confidence Interval Limits of the Mean and Single Point Future Prediction

Alloy (i)	AD (kg/m ²)	V50-VME7039 (m/s)	Conditional s, mean (m/s)	Conditional s, pred (m/s)	t	ME 95% CL (± m/s)	SPFP 95% CL (± m/s)
1	50.26	14.63	5.346	20.4	0.7173	10.72	40.9
3	51.76	67.41	5.264	20.38	3.308	10.55	40.86
2	52.43	23.61	5.231	20.37	1.159	10.49	40.84
4	54.34	63.88	5.146	20.35	3.139	10.32	40.8
3	86.02	94.82	3.253	19.95	4.752	6.522	40.01
4	91.03	70.06	3.385	19.98	3.507	6.787	40.05
3	108.90	77.14	4.556	20.21	3.818	9.134	40.51

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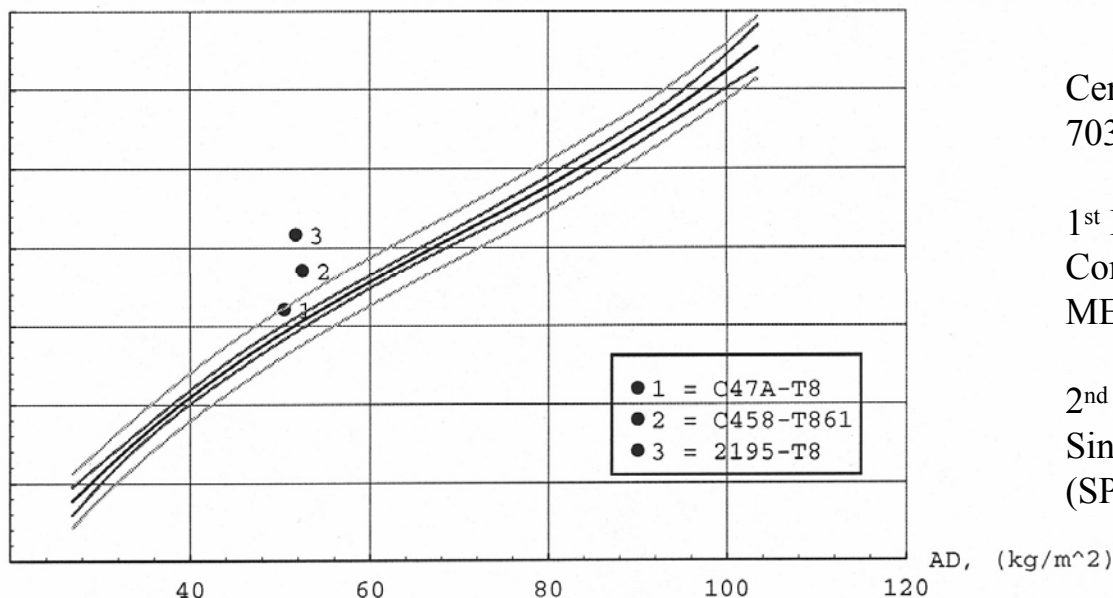


Discussion



Comparisons to 7039-T6 V50 Performance: LS Regression

V50, m/s
0.30 Cal. APM2, 30° Obliquity: Experimental Results Versus 7039-T6 Mean Estimates and 95% CLs



0.30 cal. APM2, 30°

Center (black) line = Predicted Mean
7039-T6 V50 Estimate, (ME)

1st Inner (gray) lines = 7039-T6 ME
Confidence Interval Limits = 95% (CL)
ME

2nd Outer (gray) lines = 7039-T6 CL
Single Point Future Prediction = 95% CL
(SPFP)

0.30 cal APM2, 30 deg

Exp. Results Vs 7039-T6 Mean V50 Estimates and Confidence Interval Limits of the Mean and Single Point Future Prediction

Alloy	AD	V50-VME7039	Conditional	Conditional	t	ME95% CL	SPFP 95% CL
(i)	(kg/m ²)	(m/s)	s, mean	s, pred		(± m/s)	(± m/s)
			(m/s)	(m/s)			
1	50.4	29.01	4.582	14.82	1.958	9.502	30.73
3	51.76	115.3	4.506	14.79	7.792	9.345	30.68
2	52.5	64.12	4.457	14.78	4.339	9.244	30.65

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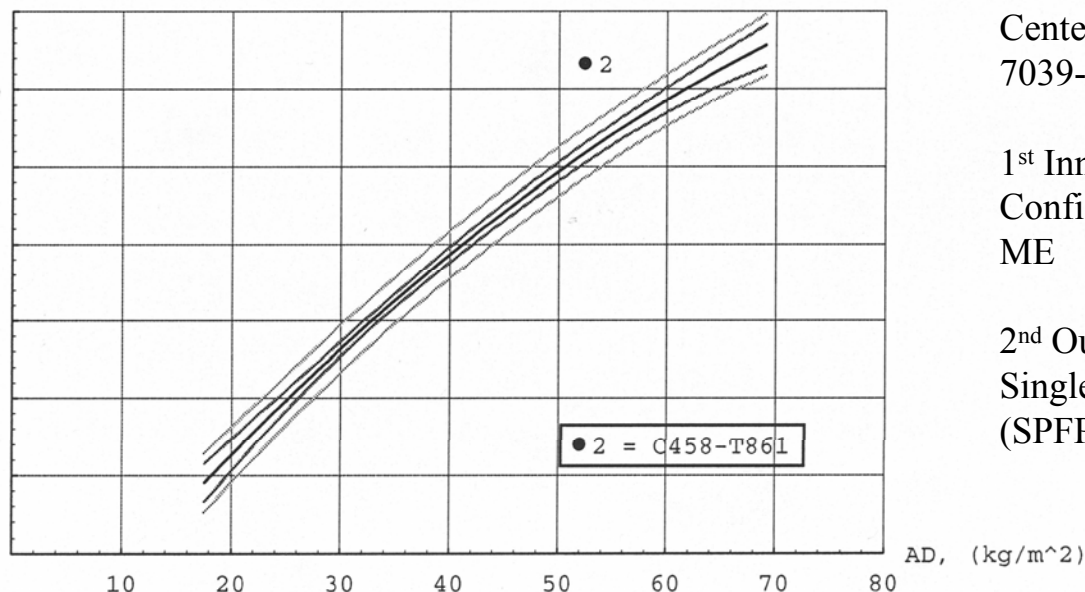
Discussion



Comparisons to 7039-T6 V50 Performance: LS Regression

0.30 cal. APM2, 45°

V50, m/s
0.30 Cal. APM2, 45° Obliquity: Experimental Results Versus 7039-T6 Mean Estimates and 95% CLs



Center (black) line = Predicted Mean
7039-T6 V50 Estimate, (ME)

1st Inner (gray) lines = 7039-T6 ME
Confidence Interval Limits = 95% (CL)
ME

2nd Outer (gray) lines = 7039-T6 CL
Single Point Future Prediction = 95% CL
(SPFP)

0.30 cal. APM2, 45 deg

Exp. Results Vs 7039-T6 Mean V50 Estimates and Confidence Interval Limits of the Mean and Single Point Future Prediction

Alloy	AD	V50-VME7039	Conditional s, mean	Conditional s, pred	t	ME 95% CL	SPFP 95% CL
(i)	(kg/m ²)	(m/s)	(m/s)	(m/s)		(± m/s)	(± m/s)
2	52.4	116.1	5.762	14.42	8.047	12.68	31.74

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Discussion



Oblique-V50 Results:

Regression-Estimate Comparisons to V50s of 0°-ADs Up-Scaled by LOS Thickness / Target Thickness (secant θ of Target Obliquity)

Proj. Obl. θ	Experimental Alloys: Oblique Results and Predicted 0° Obliquity V50s					
	Alloy	Thick. (mm)	AD, θ (kg/m ²)	Equiv. LOS at $\theta = 0^\circ$		Improvement, V50 _{θ} –LOS 0°V50 (m/s)
				Thick. (mm)	AD (kg/m ²)	
30	C47A	19.08	50.40	22.03	58.20	21.3
30	2195	19.11	51.76	22.07	59.77	55.8
30	C458	19.94	52.50	23.02	60.62	48.9
45	C458	19.90	52.40	28.14	74.10	235.9
7039-T6: Oblique and 0° Regression Predicted MEs, Reference Data						
	AD, θ (kg/m ²)		Equiv. LOS at $\theta = 0^\circ$		Improvement, V50 _{θ} –LOS 0°V50 (m/s)	
			AD (kg/m ²)			
30	50.40		58.20		7.0	
30	51.76		59.77		7.9	
30	52.50		60.62		8.4	
45	52.40		74.10		143.4	
	2519: Oblique Point Estimates and Simple Linear 0° Obliquity MEs, Reference Data					
	AD, 0° PE		Equiv. LOS at $\theta = 0^\circ$		Improvement, V50 _{θ} –LOS 0°V50	
			AD			
30	55.62		64.24		–31.7	

Notes: For 7039, LOS V50s were estimated from LOS ADs by the 0.30-cal. APM2, 0° regression equation

For experimental alloys, LOS V50s were estimated at 0° obliquity with LOS ADs and the 0.30-cal. APM2, 0° regression equation with b_0 = coefficient adjusted upward 14.63 for C47A, 23.61 for C458, and 67.41 for 2195 to fit V50 improvements of the 19- to 20-mm nominal thickness targets.

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Discussion



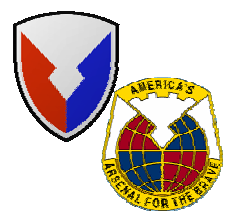
Experimental Oblique-Impact V50 vs. (LOS t / t) Scaled, 0° V50

Experimental Results, 0.30-cal. APM2 (Figure 5c-d)						V50, θ Oblique vs. $\theta = 0^\circ$ Sec(θ) Scaled Exp.		
Obliquity θ Deg. 0 and θ°	Exper. Alloy	$\theta = 0^\circ$ Exp. Data		$\theta = 30$ or 45° Exp. Data		sec θ	sec x 0°	Excess
		Thick. (mm)	AD (kg/m ²)	Thick. (mm)	AD (kg/m ²)	LOSt/ target t	AD (kg/m ²)	V500-V500°sec θ (m/s)
0 and 30°	C47A	19.02	50.26	19.08	50.40	1.155	58.20	-21.7
0 and 30°	2195	19.11	51.76	19.11	51.76	1.155	59.77	4.0
0 and 30°	C458	19.91	52.43	19.94	52.50	1.155	60.62	4.4
0 and 45°	C458	19.91	52.43	19.90	52.40	1.414	74.10	117.6
Regression of 7039-T6 vs. 0.30-cal.						V50 ME, θ Oblique vs. $\theta = 0^\circ$ Sec(θ) Scaled ME.		
Obliquity θ Deg. 0 and θ°	AD Point	$\theta = 0^\circ$ Regression		$\theta = 30, 45^\circ$ Obl. Regr.		sec θ	sec x 0°	Excess
			AD (kg/m ²)		AD (kg/m ²)	LOSt/ target t	AD (kg/m ²)	V500-V500°sec θ (m/s)
0 and 30°	C47A		50.26		50.40	1.155	58.20	-33.82
0 and 30°	2195		51.76		51.76	1.155	59.77	-33.45
0 and 30°	C458		52.43		52.40	1.155	60.62	-32.41
0 and 45°	C458		52.43		52.40	1.414	74.10	34.87
Simple Linear and Point Estimates, 2519 vs. 0.30-cal. APM2 Ref. Data						V50 PE, θ Oblique vs. $\theta = 0^\circ$ Sec(θ) Scaled SLE		
θ Deg. 0 and θ°	AD Point	$\theta = 0^\circ$ SLE Mean		$\theta = 30^\circ$ (4 PE Mean)		sec θ	sec x 0°	Excess
			AD (kg/m ²)		AD (kg/m ²)		AD (kg/m ²)	V500-V500°sec θ (m/s)
0 and 30°	2519		55.62		55.62	1.155	64.23	-37.8
2519 vs. 0.50-cal. APM2, Ref. Data						V50, θ Oblique vs. $\theta = 0^\circ$ Sec(θ) Scaled		
θ Deg. 0 and θ°	AD Point	$\theta = 0^\circ$ Ref. Data		$\theta = 45^\circ$ Ref. Data			sec x 0°	Excess
			AD (kg/m ²)		AD (kg/m ²)	sec θ	AD (kg/m ²)	V500-V500°sec θ (m/s)
0 and 45°	2519		108.8		109.3	1.414	154.5	24.4

Notes:

ME = LS Regression Mean Estimate, SLE = Straight Line Estimate), PE = (4) Point Estimate

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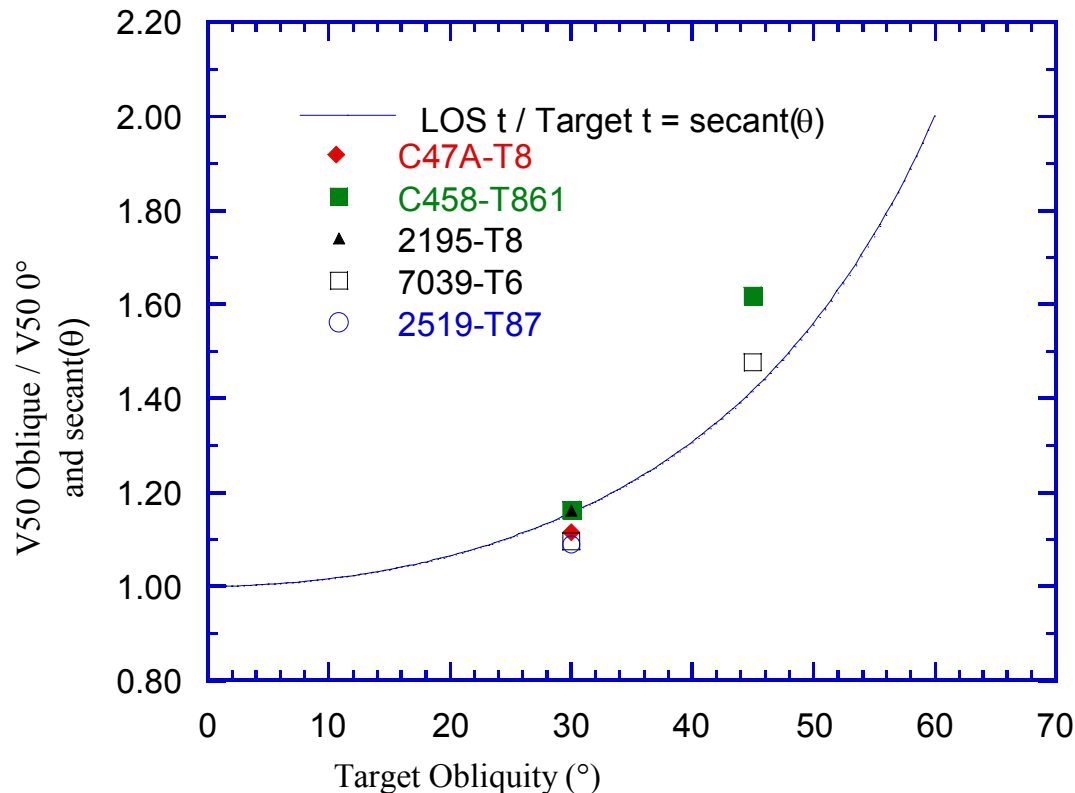


Discussion

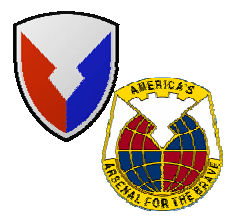


Experimental Oblique-Impact V50 vs. V50 0° and (LOS t / Target t)

0.30 cal. APM2 Oblique Performance



- 2195-T8 and C458-T861 V50 performance and mass efficiency improve with target obliquity, C4585 V50 Oblique 45° / V50 0° = 1.62 versus $\sec(\theta) = 1.414$



Conclusions



- **Al-Li Alloys: Best Specific Strengths**
- **Protection versus FSP, 0°, approximate 7039-T6 Average**
- **Superior Protection Vs AP Projectile:**
 - V50 Performance Improves with Target Strength**
 - Al-Li V50 & M_e Performance Improves w Oblique Impact**
 - * **Exceeds 7039 or 2519 performance**
 - * **Material Parameters and Failure Mode of 2195 and C458 Enhance Protection versus AP projectile**
 - * **Reduced sensitivity failure mode to increased V**
- **Damage-Tolerant, High Shot Density, Multiple Impact Capability**